

$$\begin{aligned}
 12. & \left[ \left( \frac{1}{a^2} + \frac{1}{b^2} \right) \cdot \frac{1}{a^2 + 2ab + b^2} + \frac{2}{(a+b)^3} \cdot \left( \frac{1}{a} + \frac{1}{b} \right) \right] \cdot \frac{a-b}{a^3 b^3} = \\
 & = \left[ \frac{b^2 + a^2}{a^2 b^2} \cdot \frac{1}{(a+b)^2} + \frac{2}{(a+b)^3} \cdot \frac{b+a}{ab} \right] \cdot \frac{a^3 b^3}{a-b} = \\
 & = \left[ \frac{a^2 + b^2}{a^2 b^2 (a+b)^2} + \frac{2(a+b)}{(a+b)^3 \cdot ab} \right] \cdot \frac{a^3 b^3}{a-b} = \\
 & = \frac{a^2 + b^2 + 2ab}{a^2 b^2 (a+b)^2} \cdot \frac{a^3 b^3}{a-b} = \\
 & = \frac{(a+b)^2}{a^2 b^2 (a+b)^2} \cdot \frac{a^3 b^3}{a-b} = \frac{ab}{a-b} \quad \begin{array}{l} a \neq 0 \\ b \neq 0 \\ a \neq \pm b \end{array}
 \end{aligned}$$

$$\begin{aligned}
 13. & \frac{\left( \frac{x}{y} + \frac{y}{x} - 1 \right) \left( \frac{x}{y} + \frac{y}{x} + 1 \right) (x^2 - y^2)}{=} \\
 & = \frac{\frac{x^4}{y^2} - \frac{y^4}{x^2}}{xy} \cdot \frac{x^2 + y^2 + xy}{xy} \cdot \frac{(x^2 - y^2) \cancel{(x+y)}}{=} \\
 & = \frac{(x^2 + y^2 - xy) \cdot (x^2 + y^2 + xy) \cdot (x^2 - y^2)}{x^2 y^2} \cdot \frac{x^2 y^2}{(x^2 - y^2) (x^4 + x^2 y^2 + y^4)} = \\
 & = \frac{x^4 + x^2 y^2 + x^3 y + x^2 y^2 + y^4 + xy^3 - x^3 y - xy^3 - x^2 y^2}{x^4 + x^2 y^2 + y^4} = 1 \quad \begin{array}{l} x \neq 0 \\ y \neq 0 \\ x \neq \pm y \end{array}
 \end{aligned}$$