

Goniometrické'

POH. VZOREC

$$\sin^2 x + \cos^2 x = 1 \begin{cases} \sin^2 x = 1 - \cos^2 x \\ \cos^2 x = 1 - \sin^2 x \end{cases}$$

$$\sin 2x = 2 \cdot \sin x \cdot \cos x$$

$$\cos 2x = \cos^2 x - \sin^2 x$$

$$\begin{aligned} \lim_{x \rightarrow \frac{\pi}{2}} \frac{\cos 2x + \sin^2 x}{1 - \sin x} &= \lim_{x \rightarrow \frac{\pi}{2}} \frac{\cos^2 x - \sin^2 x + 1 - \cos^2 x}{1 - \sin x} = \\ &= \lim_{x \rightarrow \frac{\pi}{2}} \frac{1 - \sin^2 x}{1 - \sin x} \stackrel{\text{VZOREC}}{=} \lim_{x \rightarrow \frac{\pi}{2}} \frac{(1 - \sin x)(1 + \sin x)}{1 - \sin x} = \lim_{x \rightarrow \frac{\pi}{2}} 1 + \sin x = \\ &= 1 + \sin \frac{\pi}{2} = 1 + 1 = 2 \end{aligned}$$

KALKULÁČKA

$$\begin{aligned} \lim_{x \rightarrow \frac{3\pi}{2}} \frac{\sin 2x + 2 \cos x}{\cos^2 x} &= \lim_{x \rightarrow \frac{3\pi}{2}} \frac{(2 \sin x \cdot \cos x + 2 \cos x)}{1 - \sin^2 x} = \\ &= \lim_{x \rightarrow \frac{3\pi}{2}} \frac{2 \cos x (\sin x + 1)}{(1 - \sin x)(1 + \sin x)} \stackrel{\text{VZOREC } A^2 - B^2 = (A - B)(A + B)}{=} \lim_{x \rightarrow \frac{3\pi}{2}} \frac{2 \cos x}{1 - \sin x} = \frac{2 \cdot \cos \frac{3\pi}{2}}{1 - \sin \frac{3\pi}{2}} = \frac{2 \cdot 0}{1 - (-1)} = 0 \end{aligned}$$

DOSADÍM